Comparison of WiFi-based indoor positioning techniques

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Abstract

Indoor positioning systems is an actively researched area of computer science. Various techniques, methods and applications were developed in the last decade. This paper gives a brief comparison of trilateration and fingerprinting techniques. Received signal strength of WiFi access points were used during the tests. Standard, genetic algorithm and simulated annealing based trilateration methods were implemented. Fingerprinting methods were based on nearest neighbor approach. Correlation coefficient and euclidean distance were used to calculate distance of the actual and the stored measurements. Experimental results showed that approximately 3–4 meter accuracy can be achieved with the tested methods.

Keywords: Indoor positioning, WiFi, trilateration, fingerprinting

MSC: AMS classification numbers

1. Introduction

Finding objects or people is crucial for various applications such as, asset tracking [11] or guidance [6]. Global and Indoor Positioning Systems are usually distinguished. The GPS is one of the most widely used Global Positioning System these days which was designed to determine the position anywhere on the Earth. GPS cannot be used in buildings due to its line of sight requirement. Indoor positioning systems aim to locate objects or people in buildings and they have been actively researched for over a decade.

Various technologies are used for indoor positioning. The first systems were based on infrared and ultrasonic technologies which can require special hardware.
development or have significant installation cost. Recent developments are based on RFID or WiFi technologies. Many access control systems use RFID tags for identification due to the low cost of passive tags and simple implementation. In localization systems the users usually have readers and the tags are placed in the building. The user only read the nearby RFID tags and the position is determined by a central server which requires communication. The popularity of the WiFi based localization system can be explained with the low installation cost. These systems use the WLAN for both localization and communication purposes. These systems are cheap to install because the WLAN networks are already established in many cases and the smartphones support WiFi communication.

This paper gives a brief comparison of two basic positioning methods: trilateration and fingerprinting. These methods are based on received signal strengths information of WiFi access points. The standard trilateration method is based on distance measurement thus the accuracy of the method depends on the distance calculation. Heuristic methods was used to handle the error of the distance calculation. Fingerprinting technique has two phases: measurement and positioning. During the measurement phase, the characteristics of the received signals are measured in known positions and the results are stored in a database. In the positioning phase, the system compares the actual and the stored measurements in order to determine the current position. Correlation coefficient and Euclidean distance were used to calculate the similarity of the current and the stored measurements.

2. Related work

Positioning and localization is an actively researched area of computer science. The existing solutions can be categorized based on various aspects, such as used technology, accuracy or environment. The indoor and outdoor positioning systems are usually distinguished. Although GPS may be the most well-known and most widely used positioning system, there are other solutions. There are systems for cell phone localization [12, 2] for example the Enhanced 911 [13].

Indoor Positioning Systems become popular about 2000. Since that, numerous indoor positioning systems have been developed [9, 8, 3]. The challenges of these systems are usually caused by the physical structure of the buildings. The existing systems are based on various technologies and principles. This paper compares only received signal strength information based techniques.

LANDMARC [10, 7] is based on RFID technology. The tags are placed in the room and the users carry the readers. The readers are connected to the server via WLAN. The distance between the tags and the reader is not determined precisely. Each reader returns with the detected RFID tags within a given range. Reference tags are used to deal with the dynamical changes of the environment. A $k$ nearest neighbor approach is used for positioning.

The RADAR system [1] is based on received signal strengths which is transmitted by the mobile device. The WLAN network is used for both measurement and communication. The localization service is implemented in the base station which
receives the signals from the mobile devices. The RADAR system has off–line and on–line phases. In the off–line phase, the signal strengths are measured in known positions. In the on–line phase, the system is used for positioning. The RADAR system uses both triangulation and signal propagation model.

The Horus system [16, 15] also based on the received signal strength information of WiFi access points. While in the RADAR system the measurements are done by the base stations, in Horus the mobile devices measures the signal strengths. It also has an off–line and an on–line phases. In the off–line phase the measurements are stored in the database which is called radio map. In the on–line phase the mobile devices measure the signal strengths then send the measurements to the server. The server use a clustering method to determine the position of the device.

3. Examined techniques

Trilateration and fingerprinting are the two major techniques of indoor positioning systems. The existing solutions are usually based on one of these techniques. The tested algorithms are detailed below.

3.1. Trilateration

Triangulation and trilateration techniques are both based on the geometrical properties of the triangle. In triangulation, the angles are used to determine the location. Trilateration technique is based on the distance of the transmitter and the receiver. In this paper only trilateration based methods are analyzed.

3.1.1. Distance approximation

The received signal strength was used to calculate the distance of the transmitters and the mobile device. This method was chosen because it does not require additional hardware components and it is easy to implement. On the other hand it can limit the accuracy of the system [5]. Free space path loss was used to calculate the distance. The calculation is based on the signal attenuation and the parameters of the environment were given.

3.1.2. Standard method

The standard trilateration is based on vector operations. The position of the access points are fix and known thus they can be represented by vectors \((a_{p_i,x}, a_{p_i,y}, a_{p_i,z})\) where \(a_{p_i}\) denotes \(i\)th the access point and \(x, y, z\) stand for the coordinates. Let \(l = (l_x, l_y, l_z)\) denote the current location and the distance between the access point and the device is calculated with Euclidean distance. In a \(n\) dimensional space \(n + 1\) points are required to determine the location of a point. Figure 1 shows both the ideal and the real cases. The ideal case is denoted by the solid line. In the ideal case the point can be determined exactly by the distances from the reference points because the distances are exactly determined. In real cases
the distance calculation is not accurate thus the position cannot be determined exactly. Moreover the different access points can have different errors.

![Figure 1: Ambiguity of Trilateration](image-url)

### 3.1.3. Heuristic approaches

The above reviewed standard method has some drawbacks. Firstly, it requires at least four reference points to determine the location. Secondly, it assumes that the distances are accurate, but in the experiments the distance between the device and the access point is approximated so it can contain error.

To deal with these limits the localization problem was transformed into an optimization task. Let us assume that, there are $n$ available reference access points in the current location. The distances can be approximated $\hat{d}(l, ap_i)$. The object function is defined as the square of the difference of the error of the approximated and calculated differences. Equation 3.1 shows the object function. Simulated annealing [14] and genetic algorithm [4] were used to solve the optimization task.

$$E(l_x, l_y, l_z) = \sum_{i=0}^{n} (d(l, ap_i) - \hat{d}(l, ap_i))^2 \rightarrow \min$$ (3.1)

### 3.2. Fingerprinting

Fingerprinting techniques usually have two phases: an off–line teaching phase and an on–line positioning phase. A fingerprinting database is used to store measurement of received signal strengths information in known position. The database can
contain one sample or even a time series [15] for each access point. In the off-line phase the database is filled. This phase can be costly and it has to be repeated if the environment changes significantly. The accuracy of the system depends on the stored measurements. In the on-line phase the location is estimated based on the received signal strengths. Both deterministic and probabilistic estimations can be used. Various pattern recognition techniques are used, such as $k$–nearest–neighbor, artificial neural network or support vector machines. The tested algorithm was based on the $k$ nearest neighbor approach.

3.2.1. Distance calculation

Correlation coefficient and Euclidean distance were used to calculate the distance of the actual and the received signal strength informations. The database is considered as two matrices. The matrix of the probe points $P$ which contains the coordinates of the measurements. The measured values are stored in the $M$ measurement matrix where the columns denote the access points and the rows are the measurements. Hence a measurement is represented by a vector $m$ which contains the signal strength of the given access point or zero if it is unavailable. These measurements and the probe points are paired.

In the current location the measurements are contained in the $m_c$ vector. The location is determined based on the similarity of the current measurement $m_c$ with the stored measurements $M$. Correlation coefficient was used to determine the similarity of two measurements and it is shown in Equation 3.2 where $m_i(k)$ is the $k$th value of the $m_i$ vector, $\overline{m}$ is the average and $s_m$ is the deviation of the $m$ measurement. Let $c$ denote a vector of correlation coefficients. Equation 3.3 shows the estimation of the current location. The method has a parameter which is the $\tau$ threshold value of correlation coefficient. If the correlation coefficient does not exceed the $\tau$ threshold, then it is considered zero thus the point is omitted.

$$cor(m_i, m_j) = \sum_{k=0}^{n} \frac{(m_i(k) - \overline{m})(m_j(k) - \overline{m})}{s_m s_m}$$

$$l_c = \frac{cP}{c}$$

Euclidean distance was used to determine the most similar neighbors. The measurements determine a point in a $n$ dimensional space where $n$ is the number of the access points. Each measurement determines a point and the similarity is determined base on the distance of the points.

4. Experimental results

A web service and a mobile client were developed to measure the accuracy of the above detailed methods. Positioning interface was defined on the server side. The tested methods implemented this interface and they were realized as web services. The mobile client was an Android application and it used HTTP requests and
JSON messages to communicate with the server. Both the server and the client side were implemented in Java.

The methods were evaluated from the point of view of accuracy. The accuracy was calculated as the difference of the determined and the actual position in meters. The measurements were performed in the same positions with the different methods. The tested methods were characterized by the minimum, maximum, average, variance and the 75th percentile of the error. Best and worst cases are represented by the minimum and the maximum error. Although average and variance are widely used to describe measurements, their interpretation can be difficult due to the outlying values. Thus the 75th percentile is used to determine the precision of the algorithms.

### 4.1. Test environment

The evaluated methods were tested in the first floor of the Institute of Information Science at the University of Miskolc. The building is approximately 48 meters long and 28 meters wide. There are two corridors and a hall on the floor. Two access points were installed at the end of the corridors and another two were placed in the hall for the measurements.

### 4.2. Trilateriation

Table 1 shows the error of the measurements with trilateriation techniques. The highest accuracy was achieved with the standard trilateriation method. The genetic algorithm based method performed poorly in our experiments but it was tested with only a couple setups. The performance of the genetic algorithm based method could be improved with the tuning. Simulated annealing based heuristic method performed well. The best average accuracy was around 3.6 meters and the 75 per cent of the measured errors were below then 4.75 meters. Experimental results shows that the standard method can be enhanced with heuristic searches which could improved the accuracy of the system.

<table>
<thead>
<tr>
<th>Method</th>
<th>Min</th>
<th>Max</th>
<th>Avg</th>
<th>Var</th>
<th>75th</th>
</tr>
</thead>
<tbody>
<tr>
<td>Standard</td>
<td>0.7083</td>
<td>10.0874</td>
<td>4.4716</td>
<td>2.7488</td>
<td>5.0971</td>
</tr>
<tr>
<td>Genetic Algorithm</td>
<td>0.9526</td>
<td>12.3559</td>
<td>5.0436</td>
<td>3.7166</td>
<td>5.3973</td>
</tr>
<tr>
<td>Simulated Annealing</td>
<td>0.8409</td>
<td>7.4148</td>
<td>3.621</td>
<td>2.3094</td>
<td>4.75</td>
</tr>
</tbody>
</table>

Table 1: Errors of Trilateriation methods

### 4.3. Fingerprinting

Tested fingerprinting method uses correlation coefficient and euclidean distance to determine the similarity of the current and the stored measurements. The tests were performed with three different setups of the correlation threshold and one
setup for the euclidean distance. The experimental results are summed up in Table 2. When the distance was calculated with the correlation coefficient, the accuracy of the algorithm increased with the threshold. On the other hand the error exceeded the 5 meters during the tests. Approximately 3 meters accuracy was achieved when euclidean distance was used.

<table>
<thead>
<tr>
<th>Method</th>
<th>Min</th>
<th>Max</th>
<th>Avg</th>
<th>Var</th>
<th>75th</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.7</td>
<td>3.3178</td>
<td>31.009</td>
<td>9.0999</td>
<td>8.687</td>
<td>8.2954</td>
</tr>
<tr>
<td>0.8</td>
<td>1.55</td>
<td>31.3002</td>
<td>6.6689</td>
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<td>5.3044</td>
</tr>
<tr>
<td>0.9</td>
<td>1.58</td>
<td>8.9208</td>
<td>4.4432</td>
<td>2.0059</td>
<td>5.13</td>
</tr>
<tr>
<td>Euclidean</td>
<td>0.34</td>
<td>18</td>
<td>4.1415</td>
<td>5.1047</td>
<td>3.0192</td>
</tr>
</tbody>
</table>

Table 2: Errors of Fingerprinting method with different thresholds

5. Conclusion

Trilateration and fingerprinting based indoor positioning techniques were reviewed in this paper. Only WiFi signal strengths were used during the measurements. The WLAN network was used for both positioning and communication. Three different trilateriation methods were tested. The standard method was enhanced with genetic algorithm and simulated annealing. The analysis of the fingerprinting technique was only focused on nearest neighbor search based solutions. Correlation coefficient and Euclidean distance were used to determine the similarity of the stored and the current measurements.

The tested methods were implemented as web services and the client was an Android device. Experimental results were compared from the point of view of accuracy. The error of the positioning methods was calculated as the difference of the actual and the determined positions. The methods were evaluated based on the minimum, maximum average, variance and 75th percentile of the errors. Approximately 3-5 meters accuracy was achieved with the tested methods.

References


